

BHARATH COACHING CENTRE

10th CBSE

Arithmetic Progressions (Series)

Total: 50

Maths

SA – II

Time: 1.30hrs

Section A

5 X 1 = 5

1. Find the sum of all even natural number less than 100.
2. In an AP, if $a = 1$, $a_n = 20$ and $S_n = 20$ and $S_n = 420$, then find the value of n .
3. Sum of first n terms of a series is $5n^2 + 2n$, find the second term of this series.
4. Find the sum of first 10 multiples of 2.
5. Find the sum of first n terms of the series $\sqrt{2} + \sqrt{8} + \sqrt{18} + \dots$

Section B

5 X 2 = 10

6. If the n^{th} term of an A.P. is $T_n = 2n + 1$; find its sum to n terms.
7. Solve: $1 + 6 + 11 + 16 + \dots + x = 148$.
8. The sum of first n terms of a certain series is given as $3n^2 - 2n$. Show that the series is an arithmetic series.
9. The sum of first six terms of an arithmetic progression is 42. The ratio of its 10th term to its 30th term is 1 : 3. Calculate the first and the thirteenth term of the A.P.
10. If the sum of m terms of an A.P. is the same as the sum of its n terms, show that the sum of its $(m + n)$ terms is zero.

Section C

5 X 3 = 15

11. How many terms of the AP: 9, 17, 25, ... must be taken to get a sum of 450?
12. The sum of first 7 terms of an AP is 10 and that of next 7 terms is 17. Find the progression.
13. If the sum of first m terms of an A.P is n and the sum of first n terms is m , then show that the sum of its first $(m + n)$ terms is $-(m + n)$.
14. If the p^{th} term of an A.P is $\frac{1}{q}$ and the q^{th} term is $\frac{1}{p}$, show that the sum of first pq terms is $\frac{(pq + 1)}{2}$.
15. Find the sum of the first $2n$ terms of the following series. $1^2 - 2^2 + 3^2 - 4^2 + \dots$

Section D

6 X 1 = 6

16. The sum of the third and seventh terms of an A.P. is 6 and their product is 8. Find the sum of first sixteen terms of the A.P.
17. If there are $(2n + 1)$ terms in A.P., then prove that the ratio of the sum of odd terms and the sum of even terms is $(n + 1) : n$.
18. The sum of the first p, q, r terms of an A.P are a, b, c respectively. Show that $\frac{a}{p}(q - r) + \frac{b}{q}(r - p) + \frac{c}{r}(p - q) = 0$
19. The ratio of the sums of m and n terms of an AP is $m^2 : n^2$. Show that the ratio of the m^{th} and n^{th} terms is $(2m - 1) : (2n - 1)$.
20. Find the sum of all numbers between 100 and 200 which are not divisible by 5.